# A general method to solve problem of blind signal separation using tensor decomposition 

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#### Abstract

The estimation of mixing matrix is a key step to solve the problem of blind signal separation. The existing algorithm can only estimate the matrix of well-determined, over-determined and under-determined in condition of sparse source. Scaling and permutation ambiguities lie in both factor matrix of tensor Parallel factors decomposition and mixing matrix in blind signal separation. With this property, the estimation of mixing matrix can be transformed into tensor parallel factors decomposition of observed signal's statistic. The decomposition can be realized by the method of alternating least squares. The theoretical analysis and simulations show that the method proposed in this paper is an efficient algorithm to estimate well-determined, over-determined and under-determined mixing matrix.


Keywords: blind signal separation (BSS), tensor, parallel factors decomposition, alternating least squares (ALS)

## 1 Introduction

Blind signal separation is an area of great interest due to its ability to separate multiple independent sources from array observations without requiring a priori knowledge of the location of sources or the geometry of sensor array [1]. Such flexibility has made BSS a potential technique in a variety of applications, such as multitalker speech separation from multimicrophone audio recordings, elimination of inter user interference in wireless communications and biomedical signals processing like ECG and EEG.

There are two steps to estimate mixture matrix. First, estimate the mixture matrix. Second, recover source signals. The accuracy of estimated mixture matrix dramatically impact the result of BSS. There are many algorithms, such as fast approximate joint diagonalization (FAJD) [2], alternating columns diagonal centres (ACDC) [3], etc., that can solve well-determined, over-determined BSS problem. But, these algorithms are not suitable for estimating under-determined mixture matrix. Underdetermined means the numbers of unknown variable exceed the equations and the matrix to be estimated is "short and fat" .To solve this problem, it is regularly assumed that the source signals are sparse in time domain or transform domain [4]. In this situation, for the clustering characteristic of sparse mixing signals, scatter diagram of the observed data assembled in direction vector of mixing matrix, and under-determined mixing matrix could be obtained by local maximization algorithm. This method is effective for separating time domain sparse signal, such as audio signals. But it is not applicable to most SubGaussian signals that are not satisfy the hypothesis of
sparseness. Delathauwer propose the method of tensor decomposition to estimate the under-determined mixture matrix, that need not the hypothesis of sparseness of source signals [5]. It is a new idea for under-determined BSS.

In this paper, the problem of estimation mixture matrix of well-determined, super-determined, under-determined is addressed by parallel factors decomposition of tensor, and the parallel factors decomposition is obtained by the method of alternating least squares.

## 2 Relation between BSS and Tensor's Parallel factors decomposition

### 2.1 MODEL OF BSS

The mixing model of BSS is below
$\mathbf{x}(t)=\mathbf{A s}(t)+\mathbf{n}(t)$,
where $\mathbf{x}(t) \in \mathbb{R}^{\prime}$ represent mixture signal vector of $J$ dimension, $\mathbf{s}(t) \in \mathbb{R}^{R}$ is source signal vector of $R$ dimension whose component is independent each other, $\mathbf{n}(t) \in \mathbb{R}^{R}$ indicate additive noise which is independent with source signal, $\mathbf{A} \in \mathbb{R}^{J \times R}$ express a full row rank matrix which is to be identified.

The identification of $\mathbf{A}$ is first step to recover source signals. There are inherent scaling and permutation uncertainty of column in estimation matrix $\mathbf{A}$. The estimation of $\mathbf{A}$ writes $\hat{\mathbf{A}}$, then these two uncertainty expressed as follow:
$\mathbf{A}=\hat{\mathbf{A}} \mathbf{P D}$,

[^0]where, $\mathbf{P}$ represent $R \times R$ permutation matrix, $\mathbf{D}$ indicate $R \times R$ non-singular diagonal matrix.

### 2.2 TENSOR'S PARALLEL FACTORS DECOMPOSITION AND ITS ESSENCE UNIQUENESS CONDITION

A tensor is a multidimensional array, and it is a higher order extensions of the matrix. There are two forms in tensor decompositions: parallel factors decomposition and tucker decomposition. Tensor decomposition is widely used in psychometrics and chemo metrics. For its powerful data analysis functions, during the last decades, researcher has begun to apply it in information area, such as signal processing, machine vision, data mining, etc.

The identification of mixing matrix can be transformed into the tensor's can conical decomposition. For elaborating this method, introduce the conception of can conical decomposition.

Definition I [6]. Outer product. The outer product of three vectors $\mathbf{u} \in \mathbb{R}^{M}, \quad \mathbf{v} \in \mathbb{R}^{N}, \quad \mathbf{w} \in \mathbb{R}^{P} \quad$ is $\underline{\mathbf{Z}} \in \mathbb{R}^{M \times N \times P}$ which is a three order tensor. It writes $\underline{\mathbf{Z}}=\mathbf{u} \circ \mathbf{v} \circ \mathbf{w}$, where each element of $\underline{\mathbf{Z}}$ can obtained by
$z_{m n p}=u_{m} v_{n} w_{p} \quad m=1, \ldots, M ;$
$n=1, \ldots, N ; p=1, \ldots, P$
Definition II [6]. Rank One Tensor. A three order tensor $\underline{\mathbf{Z}} \in \mathbb{R}^{M \times N \times P}$ is rank one if it can be written as the outer product of three vectors, i.e.

$$
\begin{equation*}
\underline{\mathbf{Z}}=\mathbf{u} \circ \mathbf{v} \circ \mathbf{w} . \tag{4}
\end{equation*}
$$

Definition III [6]. Tensor's rank. Every tensor can be expressed as a sum of rank one tensors. The rank of a general tensor $\underline{\mathbf{Y}}$ is defined to be the minimum number of rank one tensors with which it is possible to express $\underline{\mathbf{Y}}$ as a sum.

Definition IV [6]. Parallel factors decomposition. The definition of $\underline{\mathbf{Y}} \in \mathbb{R}^{M \times N \times P}$ parallel factors decomposition is
$\underline{\mathbf{Y}}=\sum_{i=1}^{\operatorname{mank}(\underline{\underline{Y}})} \mathbf{u}_{i} \circ \mathbf{v}_{i} \circ \mathbf{w}_{i}=\mathbf{U}, \mathbf{V}, \mathbf{W}$,
where, $\mathbf{u}_{i} \in \mathbb{R}^{M}, \quad \mathbf{v}_{i} \in \mathbb{R}^{N}, \quad \mathbf{w}_{i} \in \mathbb{R}^{P}, \operatorname{rank}(\underline{\mathbf{Y}})$ is the rank of tensor $\quad \underline{\mathbf{Y}} \quad$ writes $\quad I=\operatorname{rank}(\underline{\mathbf{Y}})$; $\mathbf{U}=\left[\mathbf{u}_{1}, \mathbf{u}_{2}, \ldots, \mathbf{u}_{I}\right] \quad, \quad \mathbf{V}=\left[\mathbf{v}_{1}, \mathbf{v}_{2}, \ldots, \mathbf{v}_{I}\right]$ $\mathbf{W}=\left[\mathbf{w}_{1}, \mathbf{w}_{2}, \ldots, \mathbf{w}_{I}\right]$ are factor matrix of parallel factors decomposition.

Below we discuss the essence uniqueness condition of $\underline{\mathbf{Y}}$ parallel factors decomposition. Apparently, there are inherent scaling and permutation uncertainty in factor matrix. If $\alpha_{i} \beta_{i} \gamma_{i}=1(1 \leq i \leq I)$ stands, then
$\underline{\mathbf{Y}}=\sum_{i=1}^{I}\left(\alpha_{i} \mathbf{u}_{i}\right) \circ\left(\beta_{i} \mathbf{v}_{i}\right) \circ\left(\gamma_{i} \mathbf{w}_{i}\right) \quad$ work. This is called scaling uncertainty. Supposing $\mathbf{P}$ is a $I \times I$ permutation matrix, then $\underline{\mathbf{Y}}=\mathbf{U}, \mathbf{V}, \mathbf{W}=$

UP,VP,WP work, and this is called permutation uncertainty. If there are only scaling and permutation indeterminacy in factor matrix of the tensor, then parallel factors decomposition is called uniqueness.

In conclusion, there are only scaling and permutation indeterminacy both in the factor matrix of parallel factors decomposition and the estimated mixture matrix of BSS. This common is theoretical basis for transforming the problem of estimating the mixture matrix into tensor's parallel factors decomposition.

## 3 Tensor method to estimate mixture matrix

### 3.1 MODEL TRANSFORMATION

The second-order correlation matrix of mixture signals in BSS model (1) is

$$
\begin{equation*}
\mathbf{C}_{k}=E\left[\mathbf{x}(t) \mathbf{x}^{\mathrm{T}}\left(t+\tau_{k}\right)\right]=\mathbf{A D}_{k} \mathbf{A}^{\mathrm{T}} \quad k=1, \ldots, K, \tag{6}
\end{equation*}
$$

where $\mathbf{D}_{k}=E\left[\mathbf{s}(t) \mathbf{s}^{\mathrm{T}}\left(t+\tau_{k}\right)\right]$ is a diagonal matrix. To confirm robustness of the estimation, it is supposed that $K \gg R$. Assemble a three order tensor with matrix $\mathbf{C}_{k} \in \mathbb{R}^{J \times J}$ as follows
$\underline{\mathbf{C}} \in \mathbb{R}^{J \times J \times K}:(\underline{\mathbf{C}})_{i j k}=\left(\mathbf{C}_{k}\right)_{i j}: i, j=1, \ldots, J ; k=1, \ldots, K$
Define matrix $\mathbf{D} \in \mathbb{R}^{K \times R}$ as follows
$(\mathbf{D})_{k r}=\left(\mathbf{D}_{k}\right)_{r r}, \quad k=1, \ldots, K, \quad r=1, \ldots, R$.
Then tensor $\underline{\mathbf{C}}$ can be decomposed as
$\underline{\mathbf{C}}=\sum_{r=1}^{R} \mathbf{a}_{r} \circ \mathbf{a}_{r} \circ \mathbf{d}_{r}=\mathbf{A}, \mathbf{A}, \mathbf{D}$,
where $\mathbf{a}_{r}$ and $\mathbf{d}_{r}$ are $r$-th column of $\mathbf{A}$ and $\mathbf{D}$ respectively. Equation (9) is the parallel factors decomposition of tensor $\underline{\mathbf{C}}$.

If the parallel factors decomposition of $\mathbf{C}$ is unique, then mixture matrix of BSS can be estimated with it. There provided a sufficient condition that parallel factors decomposition exists solely in literature [5]. From the sufficient condition, when the number of receiving sensor is constant, the maximum of source signal that can guarantee uniqueness of parallel factors decomposition, can be deduced.

TABLE 1 Relation between sensor number J and maximum of source number $\mathrm{R}_{\text {max }}$ allowed

| $\mathbf{J}$ | 2 | 3 | 5 | 8 | 10 | 15 | 18 | 23 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{R}_{\text {max }}$ | 2 | 4 | 10 | 26 | 41 | 92 | 132 | 216 |

From Table 1 we can see that, fixing the number of receiving sensor $J$, so long as the number of source signal satisfies $R \leq R_{\max }$, the method of parallel factors decomposition can be used to estimate mixture matrix. So, tensor method can estimate the mixture matrix of welldetermined, super-determined and under-determined.

## 4 Alternating least squares (ALS) algorithm to realize parallel factors decomposition

In this section, we realize parallel factors decomposition by minimizing the cost function. Choose function follows as

$$
\begin{equation*}
f(\mathbf{A}, \mathbf{D})=\left\|\underline{\mathbf{C}}-\sum_{r=1}^{R} \mathbf{a}_{r} \circ \mathbf{a}_{r} \circ \mathbf{d}_{r}\right\|_{F}^{2} . \tag{10}
\end{equation*}
$$

For this multi-variable optimization problem, cyclic minimizing is a common method. The thought of this method is, partitioning variable set into several subsets, utilize optimization algorithm to calculate one of subsets in every step, and regard other subsets as constant, repeat this process until cost function is convergence.

In accordance with the Equation (10), we adopt ALS algorithm to realize cyclic minimizing.

The first, second and third slice matrix of tensor $\underline{\mathbf{C}}$ are respectively

$$
\begin{align*}
& \mathbf{E}_{i} \in \mathbb{R}^{J \times K}, i=1, \ldots, J  \tag{11}\\
& \mathbf{F}_{j} \in \mathbb{R}^{K \times J}, j=1, \ldots, J  \tag{12}\\
& \mathbf{G}_{k} \in \mathbb{R}^{J \times J}, k=1, \ldots, K . \tag{13}
\end{align*}
$$

Combining Equation (9) and symmetry of tensor $\underline{\mathbf{C}}$, we can deduce
$\mathbf{G}_{k}=\mathbf{A} \operatorname{diag}_{k}(\mathbf{D}) \mathbf{A}^{\mathrm{T}}, \quad k=1, \ldots, K ;$
$\mathbf{E}_{i}=\mathbf{A} \operatorname{diag}_{i}(\mathbf{A}) \mathbf{D}^{\mathrm{T}}, \quad i=1, \ldots, J ;$
$\mathbf{F}_{j}=\mathbf{D} \operatorname{diag}_{j}(\mathbf{A}) \mathbf{A}^{\mathrm{T}}, \quad j=1, \ldots, J$.
Equation (14) can be rewritten as

$$
\left[\begin{array}{c}
\mathbf{G}_{1}  \tag{17}\\
\mathbf{G}_{2} \\
\vdots \\
\mathbf{G}_{K}
\end{array}\right]=\left[\begin{array}{c}
\mathbf{A} \operatorname{diag}_{1}(\mathbf{D}) \\
\mathbf{A} \operatorname{diag}_{2}(\mathbf{D}) \\
\vdots \\
\mathbf{A} \operatorname{diag}_{K}(\mathbf{D})
\end{array}\right] \mathbf{A}^{\mathrm{T}} .
$$

From Equation (17), least square estimation of mixing matrix $\mathbf{A}$ can be inferred as

$$
\hat{\mathbf{A}}^{\mathrm{T}}=\left[\begin{array}{c}
\mathbf{A} \operatorname{diag}_{1}(\mathbf{D})  \tag{18}\\
\mathbf{A} \operatorname{diag}_{2}(\mathbf{D}) \\
\vdots \\
\mathbf{A} \operatorname{diag}_{K}(\mathbf{D})
\end{array}\right]^{\dagger}\left[\begin{array}{c}
\mathbf{G}_{1} \\
\mathbf{G}_{2} \\
\vdots \\
\mathbf{G}_{K}
\end{array}\right],
$$

where symbol " $\dagger$ " denotes moore-penrose inverse matrix. Similarly, least square estimation of $\mathbf{D}$ and $\mathbf{A}$ can be obtained respectively as
$\hat{\mathbf{D}}^{\mathrm{T}}=\left[\begin{array}{c}\mathbf{A} \operatorname{diag}_{1}(\mathbf{A}) \\ \mathbf{A} \operatorname{diag}_{2}(\mathbf{A}) \\ \vdots \\ \mathbf{A} \operatorname{diag}_{J}(\mathbf{A})\end{array}\right]^{\dagger}\left[\begin{array}{c}\mathbf{E}_{1} \\ \mathbf{E}_{2} \\ \vdots \\ \mathbf{E}_{J}\end{array}\right]$,
$\hat{\mathbf{A}}^{\mathrm{T}}=\left[\begin{array}{c}\mathbf{D} \operatorname{diag}_{1}(\mathbf{A}) \\ \mathbf{D} \operatorname{diag}_{2}(\mathbf{A}) \\ \vdots \\ \mathbf{D} \operatorname{diag}_{J}(\mathbf{A})\end{array}\right]^{\dagger}\left[\begin{array}{c}\mathbf{F}_{1} \\ \mathbf{F}_{2} \\ \vdots \\ \mathbf{F}_{J}\end{array}\right]$.
Random initialize matrix $\mathbf{A}$ and $\mathbf{D}$, then update $\hat{\mathbf{A}}$ and $\hat{\mathbf{D}}$ according to Equations (18), (19) and (20). In process of updating, $\mathbf{A}$ and $\mathbf{D}$ on the right side of equation are replaced by $\hat{\mathbf{A}}$ and $\hat{\mathbf{D}}$ that are obtained by last step of estimation.

## 5 Simulation results

In this section, we will compare the performance of our proposed method with the other algorithms presented in paper [2, 3]. We mark algorithm in this paper, in paper [2], [3] respectively as GTCD, FAJD and ACDC.

To measure the difference between the mixing matrix and the estimated matrix, the performance index, called the relative error (REER), is adopted. The REER has been frequently used in the evaluation in area of BSS [7]. The REER is given by
$R E E R=\mathrm{E}\left\{\frac{\|\mathbf{A}-\hat{\mathbf{A}}\|_{\mathrm{F}}}{\|\mathbf{A}\|_{\mathrm{F}}}\right\}$,
where, $\hat{\mathbf{A}}$ is the estimation of mixing matrix $\mathbf{A}$, under the condition that their columns are unitized and are eliminated permutation indeterminacy. For the convenience of comparing, transform the REER into decibel ( dB ) using equation $10 \log _{10}($ REER $)$. It is evident that, lower the decibel of relative error is, precise the estimation of mixing matrix is.

The second-order correlation matrices are generated by Equation (6), where the mixing matrix $\mathbf{A}$ is $M \times N$, diagonal matrix $\mathbf{D}_{k}$ is $N \times N$, and their elements are random generated with standard normal distribution in each experiment. These matrices are assembled into third order tensor $\mathbf{C} \in \mathbb{R}^{M \times M \times K}$ following Equation (7).

Experiments 1. In this experiment, we compare the performance of estimation well-determined matrix between the GTCD algorithm and FAJD algorithm based on non-unitary joint diagonalization. Assume the number of correlation function $K=100$. The iteration stop condition is set as
$\left|\left(f_{n}\left(\hat{\mathbf{A}}^{\prime}, \hat{\mathbf{D}}^{\prime}\right)-f_{n-1}\left(\hat{\mathbf{A}}^{\prime}, \hat{\mathbf{D}}^{\prime}\right)\right) / f_{n}\left(\hat{\mathbf{A}}^{\prime}, \hat{\mathbf{D}}^{\prime}\right)\right|<10^{-6}$
where the definition of $f$ function follows Equation (10).
Note: 1) The unit of Runtime is seconds. 2) REER is measured with dB . The same below.

Estimate the mixing matrix of different $M$ using algorithm GTCD and FAJD respectively, and each scenario is repeated 100 times independently. The mean of REER and run time in each case are presented in Table 2. The table illustrates that the accuracy of GTCD is better than that of FAJD. Except the low dimension case, such as $M=N=4, M=N=6$, the run time of FAJD outnumber GTCD. And the run time of FAJD rapid
increase with the dimension augment of mixing matrix.
Experiments 2. In this experiment, we compare the performance of estimation super-determined matrix between the GTCD algorithm and ACDC algorithm, based on non-unitary joint diagonalization. Set different value of $M$ and $N$ satisfying $M>N$ and independently repeat 100 times. The mean of REER and run time in each case are presented in Table 3. As can be seen from the table that, in each case, the precision of GTCD is better than that of ACDC and the run time of ACDC outnumber TCD. Similar to experiment 1 , the run time of FAJD rapid increase with the dimension augment of mixing matrix.

TABLE 2 Accuracy and runtime of two algorithms in well-determined case

|  | $\mathrm{M}=6, \mathrm{~N}=6$ |  | $\mathrm{M}=10, \mathrm{~N}=10$ |  | $\mathrm{M}=16, \mathrm{~N}=16$ |  | $\mathbf{M}=\mathbf{2 0}, \mathrm{N}=20$ |  | $\mathrm{M}=40, \mathrm{~N}=40$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | REER | Runtime | REER | Runtime | REER | Runtime | REER | Runtime | REER | Runtime |
| GTCD | -155.5 | 1.2034 | -156.3 | 1.2655 | -161.8 | 1.4023 | -156.5 | 1.8284 | -155.1 | 7.4014 |
| FAJD | -95.4 | 0.1764 | -92.6 | 0.7216 | -96.2 | 2.7487 | -82.2 | 10.1810 | -11.0 | 423.3555 |

TABLE 3 Accuracy and runtime of two algorithms in super-determined case

|  | $\mathrm{M}=6, \mathrm{~N}=4$ |  | $\mathrm{M}=10, \mathrm{~N}=6$ |  | $\mathrm{M}=16, \mathrm{~N}=10$ |  | $\mathrm{M}=20, \mathrm{~N}=12$ |  | $\mathrm{M}=40, \mathrm{~N}=30$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | REER | Runtime | REER | Runtime | REER | Runtime | REER | Runtime | REER | Runtime |
| GTCD | -345.4 | 0.3042 | -339.4 | 0.3770 | -321.6 | 0.5089 | -330.9 | 0.6537 | -306.7 | 3.0930 |
| ACDC | -84.4 | 1.4134 | -95.9 | 2.4805 | -100.9 | 7.8012 | -107.1 | 13.9125 | -121.91 | 158.4669 |

TABLE 4 Accuracy and runtime of GTCD in under-determined case

|  | $\mathbf{M}=\mathbf{4}, \mathbf{N}=\mathbf{5}$ | $\mathbf{M}=\mathbf{5}, \mathbf{N}=\mathbf{6}$ | $\mathbf{M}=\mathbf{6}, \mathbf{N}=\mathbf{8}$ | $\mathbf{M}=\mathbf{8}, \mathbf{N}=\mathbf{1 0}$ | $\mathbf{M}=\mathbf{1 0}, \mathbf{N}=\mathbf{1 6}$ | $\mathbf{M}=\mathbf{1 5}, \mathbf{N}=\mathbf{2 0}$ | $\mathbf{M}=\mathbf{1 8}, \mathbf{N}=\mathbf{3 0}$ | $\mathbf{M}=\mathbf{2 3}, \mathbf{N}=\mathbf{4 0}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| REER | -155.1 | -149.4 | -146.5 | -144.2 | -140.0 | -134.6 | -111.3 | -72.6 |
| Runtime | 1.4748 | 1.5918 | 2.5185 | 3.0151 | 4.2947 | 5.4100 | 9.1283 | 15.6118 |

Experiments 3. The performance of GTCD algorithm for estimating under-determined mixing matrix is analysed in this experiment. Assume different value of $M$ and $N$ and independently repeat 100 times in each case. The mean of REER and run time are illustrate in Table 4. It is indicated that the GTCD can address the problem of underdetermined BSS, but the ACDC and FAJD cannot resolve this problem.

## 6 Conclusion

In this paper, the estimation of mixing matrix is transformed into the problem of tensor parallel factors

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decomposition. Tensor decomposition is achieved by ALS algorithm. The proposed method not only can estimate the mixing matrix of well-determined and super-determined, but also can address under-determined matrix. The experiments show that the accuracy and the run time of our algorithm is improver than that of the existing algorithm based on non-unitary joint diagonalization.

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